

# Net radiation

## Definition

Net radiation is an input variable of the [potential evapotranspiration](#) equation formulated by [Penman \(1948\)](#).

"Net radiation is the difference between incoming and outgoing radiation of both short and long wavelengths. It is the balance between the energy absorbed, reflected and emitted by the earth's surface or the difference between the incoming net shortwave and the net outgoing longwave radiation. Net radiation is normally positive during the daytime and negative during the nighttime. The total daily value for net radiation is almost always positive over a period of 24 hours, except in extreme conditions at high latitudes" ([Allen et al. 1998](#)).

## Formula

The calculation of the net radiation requires the following steps (cf. [Allen et al. 1998](#)).

### Extraterrestrial radiation

The daily extraterrestrial radiation  $R_a = [\text{MJ}\cdot\text{m}^{-2}\cdot\text{d}^{-1}]$  has to be calculated as follows ([Allen et al. 1998](#)):

$$R_a = \frac{24 \cdot 60}{\pi} \cdot G_{sc} \cdot d_r \cdot [\omega_s \cdot \sin \varphi \cdot \sin \delta + \cos \varphi \cdot \cos \delta \cdot \sin \omega_s]$$

where  $G_{sc}$  is the solar constant, which is equal to  $0.082 [\text{MJ}\cdot\text{m}^{-2}\cdot\text{min}^{-1}]$ ,  $d_r$  the inverse relative distance Earth-Sun,  $\omega_s$  the sunset hour angle [rad],  $\varphi$  the latitude [rad], and  $\delta$  the solar declination [rad].

The inverse relative distance Earth-Sun  $d_r$  is calculated as follows:

$$d_r = 1 + 0.033 \cdot \cos\left(\frac{2\pi}{365} \cdot J\right)$$

where  $J$  is the number of the day in the year between 1 (1 January) and 365 or 366 (31 December).

The sunset hour angle  $\omega_s$  [rad] is calculated as follows:

$$\omega_s = \arccos[-\tan \varphi \cdot \tan \delta]$$

and the solar declination [rad]  $\delta$  as follows:

$$\delta = 0.409 \cdot \sin\left(\frac{2\pi}{365} \cdot J - 1.39\right)$$

The conversion from decimal degrees to radians is obtained as follows:

$$[\text{Radians}] = \frac{\pi}{180} [\text{decimal degrees}]$$

## Solar radiation

The solar radiation  $R_s$  [ $\text{MJ}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$ ] can be calculated based on the Angstrom formula (Allen et al. 1998):

$$R_s = \left( a_s + b_s \cdot \frac{n}{N} \right) \cdot R_a$$

where  $n$  is the actual duration of sunshine [hours],  $N$  the daylight hours [hours], and  $R_a$  the extraterrestrial radiation [ $\text{MJ}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$ ].  $a_s$  is a regression constant expressing the fraction of extraterrestrial radiation reaching the earth on an overcast day ( $n = 0$ ).  $a_s + b_s$  is the fraction of extraterrestrial radiation reaching the earth on a clear day ( $n = N$ ). When no actual solar radiation data are available, the values  $a_s = 0.25$  and  $b_s = 0.50$  are recommended (Allen et al. 1998).

Solar radiation  $R_s$  can also be derived from air temperature differences as follows (Allen et al. 1998):

$$R_s = R_a \cdot k_{R_s} \cdot \sqrt{T_{max} - T_{min}}$$

where  $R_a$  is the extraterrestrial radiation [ $\text{MJ}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$ ],  $k_{R_s}$  an adjustment coefficient [ $^{\circ}\text{C}^{-0.5}$ ] which is usually comprised between 0.16 ("interior" locations) and 0.19 ("coastal" locations),  $T_{max}$  maximum air temperature [ $^{\circ}\text{C}$ ] and  $T_{min}$  minimum air temperature [ $^{\circ}\text{C}$ ].

## Clear-sky solar radiation

The clear-sky solar radiation  $R_{so}$  [ $\text{MJ}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$ ] can be calculated as follows when  $a_s$  and  $b_s$  values (cf. solar radiation?) are not available (Allen et al. 1998):

$$R_{so} = (0.75 + 2 \cdot 10^{-5} \cdot z) \cdot R_a$$

where  $z$  is elevation above sea level [m].

## Net shortwave radiation

The net shortwave radiation  $R_{ns}$  [ $\text{MJ}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$ ] is calculated as follows (Allen et al. 1998):

$$R_{ns} = (1 - \alpha) \cdot R_s$$

where  $\alpha$  is the albedo or canopy reflection coefficient, which is usually between 0.20 and 0.25 for green vegetation covers, and  $R_s$  the incoming solar radiation? [ $\text{MJ}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$ ].

## Net longwave radiation

The net longwave radiation  $R_{nl}$  [ $\text{MJ}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$ ] is calculated as follows (Allen et al. 1998):

$$R_{nl} = \sigma \cdot \left( \frac{T_{max}^4 + T_{min}^4}{2} \right) \cdot (0.34 - 0.14 \cdot \sqrt{e_a}) \cdot \left( 1.35 \cdot \frac{R_s}{R_{so}} - 0.35 \right)$$

where  $\sigma$  is the Stefan-Boltzmann constant, which is equal to  $4.903 \cdot 10^{-9}$  [ $\text{MJ}\cdot\text{K}^{-4}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$ ],  $T_{max}$  and  $T_{min}$  maximal and minimal temperature [K] during the 24-hr period,  $e_a$  actual vapor pressure [kPA],  $R_s$  solar radiation? [ $\text{MJ}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$ ], and  $R_{so}$  clear-sky solar radiation? [ $\text{MJ}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$ ].

$\frac{R_s}{R_{so}}$  is limited to 1.

## Net radiation

Finally, the net radiation  $R_n$  [ $\text{MJ}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$ ] can be calculated as follows (Allen et al. 1998):

$$R_n = R_{ns} - R_{nl}$$

where  $R_{ns}$  [ $\text{MJ}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$ ] is net shortwave radiation? and  $R_{nl}$  [ $\text{MJ}\cdot\text{m}^{-2}\cdot\text{d}^{-1}$ ] net longwave radiation.

## Reference

Allen et al. (1998)

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